

CHAPTER 1/2 $\rightarrow F_e = \frac{kq_1 q_2}{r^2}$

$$\vec{F} = \frac{Fe}{q_0}, \vec{E} = \frac{kQ}{r^2}$$

CHAPTER 3 \rightarrow GAUSS' LAW

$$\star E_0 \phi = \rho_{\text{enc}}, \phi \propto \vec{E} \cdot d\vec{A}$$

$$\vec{E} @ \text{particle} \rightarrow E = \frac{\sigma}{\epsilon_0}$$

$$\vec{E} @ \infty \text{ line} \rightarrow E = \frac{\lambda}{2\pi \epsilon_0 r}$$

$$\vec{E} @ \infty \text{ sheet} \rightarrow E = \frac{\sigma}{2\epsilon_0}$$

$$\text{Outside sphere} \rightarrow E = \frac{kq}{r^2}$$

$$\text{Inside sphere} \rightarrow E = \frac{kq}{r^2}$$

CHAPTER 4 \rightarrow ELECTRIC POTENTIAL

$$V = -\frac{W_{\text{ext}}}{q_0} = \frac{U}{q_0}, U = qV$$

$$K = -q \Delta V + V_{\text{app}}$$

$$V_f - V_i = - \int E \cdot ds$$



$$\Delta V = -E \Delta x$$

$$\text{PD due to each particle} \rightarrow V = \frac{kq}{r}$$

$$V = qk \int \frac{dr}{r}, t = -\frac{\Delta V}{ds}$$

$$U = W = \frac{kq_1 q_2}{r} \text{ for each PAIR}$$

CHAPTER 5 \rightarrow CAPACITANCE

$$Q = CV = \epsilon_0 \phi EdA, \epsilon = k\epsilon_0$$

$$\text{Parallel Plate} \rightarrow C = \frac{\epsilon_0 A}{d} \quad \star$$

$V \text{ in } II$

$$\text{Cylinder} \rightarrow C = \frac{2\pi \epsilon_0 L}{\ln(b/a)} \quad Q \text{ in } \frac{1}{I}$$

$$\text{Sphere} \rightarrow C = 4\pi \epsilon_0 \frac{a}{b-a}$$

$$\text{Isolated Sphere} \rightarrow 4\pi \epsilon_0 R$$

CHAPTER 6 $\rightarrow i = \int J \cdot dA$

$$J = (ne) V_d, V = IR \quad \star$$

$$(I_c = \frac{1}{2} CV^2) \quad \star$$

$$\rho = \frac{1}{\sigma} = \frac{E}{J}, R = \rho \frac{L}{A} \quad \begin{matrix} \text{density always} \\ \text{points in} \\ \text{direction of} \\ \text{conventional} \\ \text{current.} \end{matrix}$$

$$\rho - \rho_0 = \rho \alpha (T - T_0)$$

$$\rho = \frac{m}{e^2 n C} \quad P = iV = iR = \frac{V^2}{R}$$

CHAPTER 7/8 \rightarrow MAGNETISM

$$F_B = q \vec{v} \times \vec{B} = i \vec{L} \times \vec{B} \rightarrow \text{right hand rule}$$

$$qVB = \frac{mv^2}{R} \rightarrow r = \frac{mv}{qB}$$

$$f = \frac{\omega}{2\pi} = \frac{1}{T} = \frac{q}{B2m}$$

Biot-Savart Law

$$G \cdot dB = \frac{\mu_0 i}{4\pi r} = \frac{i ds \times \hat{r}}{r^2}$$

$$B_{\text{wire}} = \frac{\mu_0 i}{2\pi R}$$

$$B_{1/2 \text{ wire}} = \frac{\mu_0 i}{4\pi R}$$

$$B_{\text{arc}} = \frac{\mu_0 i l}{4\pi R} \text{ (RAD'S!)}$$

$$\text{Parallel } I \Rightarrow F_B = \frac{\mu_0 I i \sin \theta}{2\pi d}$$

Same attracts, opp repels

AMPERE'S LAW

$$\oint B ds = i_{\text{enc}}$$

$$B = \frac{\mu_0 i N}{l} \text{ (solenoid)}$$

$$B = \frac{\mu_0 i N}{2\pi R} \text{ (toroid)}$$

N = turns / metre

$$E = BLV$$

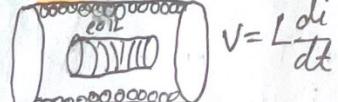
$$L = \frac{BLN}{R}, P = B^2 L^2 V^2$$

$$E = \oint E \cdot ds$$

$$E = -N \frac{d\Phi_B}{dt}$$

$$L = \frac{N \Phi_B}{c} \rightarrow L = \mu_0 N^2 A / \text{(solenoid)}$$

SOLENOID



$$V = L \frac{di}{dt}, i = C \frac{dv}{dt}$$

$$B = \frac{\mu_0 i N}{c} \text{ (solenoid)}$$

$$\Phi_B = NBA \text{ (coil)}$$

$$E = -N \frac{d\Phi_B}{dt}$$

* HALL EFFECT \rightarrow PD due to current in wire w/ B

\rightarrow i * GARNSHAW \rightarrow No system of free particles can reach equilibrium

* FARADAY'S LAW \rightarrow Change in E in loop induces current in loop

* LENZ'S LAW \rightarrow Induced current will produce B to oppose change in external B.

* TELEGEN'S THEOREM $\rightarrow \sum P = 0$ for any network

CIRCUITS \rightarrow MISCELLANEOUS

KCL $\rightarrow \sum I = 0$ for a node

KVL $\rightarrow \sum V = 0$ for a closed loop

Max Power \rightarrow when $R_L = R_{\text{th}} = \frac{V^2}{4R_{\text{th}}}$

Current division $\rightarrow I_1 = \frac{R_2}{R_1 + R_2} I_0$

Voltage division $\rightarrow V_1 = \frac{R_L}{R_1 + R_2} V_0$

- TECHNIQUES
- ① NODAL
- ② LOOP
- ③ SUPERPOSITION
- ④ THEVENIN
- ⑤ NORTON
- ⑥ SOURCE TRANSFORMATION

Nodal Analysis $\rightarrow N-1$ equations

Loop Analysis $\rightarrow B-N+1$ equations

TRANSIENT CIRCUITS

CAPACITOR CHARGED \rightarrow Voltage $V(t) = \frac{1}{2} C V^2 = \frac{1}{2} C I^2$ (open)

INDUCTOR DISCHARGED \rightarrow Current $I(t) = I_0 e^{-t/L} = I_0 e^{-t/R_{\text{th}}}$ (short)

INDUCTOR CHARGED \rightarrow Current $I(t) = I_0 e^{t/L} = I_0 e^{t/R_{\text{th}}}$ (open)

$U = \frac{1}{2} CV^2 = \frac{1}{2} Li^2$

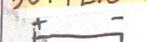
Capacitor $\rightarrow T = R_{\text{th}} C$

Inductor $\rightarrow T = L/R_{\text{th}}$

$V = L \frac{di}{dt}, i = C \frac{dv}{dt}$

$V_C = \frac{di_C}{dt}, i_C = \frac{dv_C}{dt}$

SUPPLIED

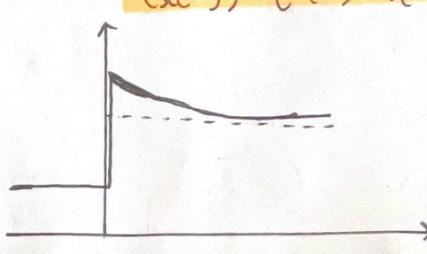


ABSORBED



$$x(t) = K_1 + K_2 e^{-t/T}$$

$$= (x(\infty)) + (V(0^+) - V(\infty)) e^{-t/T}$$



CONSTANTS

$$\text{Electric Constant} \rightarrow k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \frac{\text{N m}^2}{\text{C}^2}$$

$$\text{Permittivity of Free Space} \rightarrow \epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2}$$

$$\text{Clementry Charge} \rightarrow 1.602 \times 10^{-19} \text{ C}$$

$$\text{Electron Mass} \rightarrow 9.11 \times 10^{-31} \text{ kg}$$

$$\text{Proton/Neutron Mass} \rightarrow 1.67 \times 10^{-27} \text{ kg}$$

$$\text{Permeability} \rightarrow \mu_0 = 4\pi \times 10^{-7} \frac{\text{N}}{\text{A}^2} = 12.566 \times 10^{-7}$$

UNITS

$$\text{Current} \rightarrow A = \frac{C}{S}$$

$$\text{Electric Field} \rightarrow \frac{N}{C} = \frac{V}{m}$$

$$\text{Electric Flux} \rightarrow Vm$$

$$\text{Capacitance} \rightarrow F = C/V$$

$$\text{Resistance} \rightarrow \Omega = \frac{V}{A}$$

$$\text{Resistivity} \rightarrow \Omega m$$

$$\text{Power} \rightarrow W = \frac{J}{S}$$

$$\text{Mag Field} \rightarrow T = \frac{N}{A \cdot m}$$

$$\text{Mag Flux} \rightarrow \Phi_B = T \cdot m^2$$

$$\text{Inductance} \rightarrow H = \frac{T \cdot m^2}{A}$$

$$\text{Sine Law} \rightarrow \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\text{Cosine Law} \rightarrow c^2 = a^2 + b^2 - 2ab \cos \theta$$

$$\text{Sphere} \rightarrow V = \frac{4}{3}\pi R^3, SA = 4\pi R^2$$

$$\text{Cylinder} \rightarrow V = \pi R^2 h, SA = 2\pi r(r+h)$$

PARALLEL SERIES

$$C \quad \sum C_j \quad \frac{1}{\sum C_j}$$

$$R \quad \sum \frac{1}{R_j} \quad \sum R_j$$

$$L \quad \sum \frac{1}{L_j} \quad \sum L_j$$

$$\Sigma \quad \sum \frac{1}{Z_j} \quad \sum Z_j$$

AC CIRCUITS

$$Z = R(\omega) + jX(\omega)$$

resistance reactance

inverse of resistance \rightarrow conductance
inverse of reactance \rightarrow susceptance
inverse of impedance \rightarrow admittance

$$\xrightarrow{+1 \Omega} Z = R$$

$$\xrightarrow{v(t) = R i(t)}$$

$$\xrightarrow{-j \Omega} Z = j\omega L = jX_L$$

$$\xrightarrow{\frac{1}{T} \rightarrow v(t) = \frac{1}{C} \int_{-\infty}^t i(x) dx}$$

$$\xrightarrow{j \Omega} Z = \frac{1}{j\omega C} = -j\omega C = jX_C$$

$$\xrightarrow{\frac{1}{C} \rightarrow i(t) = \frac{1}{L} \int_{-\infty}^t v(x) dx}$$

PHASOR RELATIONSHIPS

Resistors $\rightarrow \Theta_v = \Theta_i \rightarrow$ always in phase

Capacitors $\rightarrow \Theta_v = \Theta_i + 90^\circ \rightarrow$ voltage leads by 90°

Inductors $\rightarrow \Theta_i = \Theta_v + 90^\circ \rightarrow$ current leads by 90°

PHASOR NOTATION & ARITHMETIC

$A \cos(\omega t + \theta) = A \angle \theta \rightarrow$ Phase angles based off cosine

$\omega \sin \theta = \sin(\theta + 90^\circ) \text{ AND } \sin \theta = \cos(\theta - 90^\circ)$

* Angular frequency is common factor, do not consider in solving.

$$\text{ADMITTANCE} \rightarrow Y = \frac{1}{Z}$$

$$\omega = 2\pi f$$

$$R \rightarrow Y_R = 1/A = G$$

$$L \rightarrow Y_L = 1/j\omega L = -1/\omega L \angle 90^\circ$$

$$C \rightarrow Y_C = j\omega C = \omega C \angle 90^\circ$$

CRAMER'S RULE

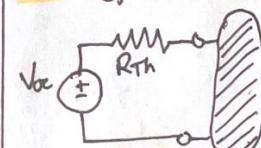
$$\begin{bmatrix} j2 & 4+j3 \\ 10-j6 & j2 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 10L \\ 0 \end{bmatrix}$$

$$I_1 = \frac{D_1}{\Delta} = \frac{|E \ B|}{|A \ B|} = \frac{ED - BF}{AD - BC}$$

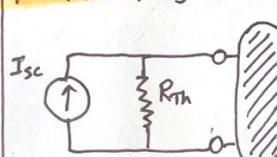
$$I_2 = \frac{D_2}{\Delta} = \frac{|A \ E|}{|A \ B|} = \frac{AF - EC}{AD - BC}$$

If asked for Thévenin equivalent at terminals, INCLUDE. If asked for Thévenin voltage across (load) resistor, don't include.

THEVENIN'S THEOREM



NORTON'S THEOREM



SOURCE TRANSFORMATION

* Technique to simplify Thévenin and Norton Theorems

THREE TYPES OF THEVENINS

① Indy ONLY \rightarrow zero all sources

② Dep ONLY \rightarrow inject voltage

③ BOTH \rightarrow find V_{oc} & I_{sc} $R_{th} = \frac{V_{oc}}{I_{sc}}$